# Cerium(IV) Oxide Sulphate Hydrate, a New Refinement 

By Ove Lindgren<br>Department of Inorganic Chemistry, Chalmers University of Technology and the University of Gothenburg, P.O. Box, S-402 20 Göteborg, Sweden

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#### Abstract

CeOSO}_{4} . \mathrm{H}_{2} \mathrm{O}\), orthorhombic, $P 2_{1} 2_{1} 2_{1}, Z=4$, $a=11.987$ (2), $b=8.272$ (2), $c=4.331$ (1) $\AA, \quad V=$ $429 \cdot 1 \AA^{3}, \mu(\mathrm{Mo} K \alpha)=101 \cdot 0 \mathrm{~cm}^{-1}, \quad D_{x}=4 \cdot 182, \quad D_{m}=$ $4 \cdot 2 \mathrm{~g} \mathrm{~cm}^{-3}$. The structure was reported previously [Lundgren, Ark. Kem. (1953), 5, 59-75], and is built up by infinite strings of $\left(\mathrm{CeO}^{2+}\right)_{n}$ parallel to $\mathbf{c}$, crosslinked by $\mathrm{SO}_{4}$ groups. New intensities ( 2411 non-zero reflexions) have been refined by least squares to a final $R$ of $0 \cdot 030$.


Introduction. Yellow prismatic crystals (elongation c) were obtained by hydrothermal hydrolysis of a $\mathrm{Ce}^{\mathrm{iv}}$ sulphate solution (Lundgren, 1953). A specimen, $0.24 \times 0.17 \times 0.47 \mathrm{~mm}$, was mounted on a Pailred single-crystal diffractometer with graphite-monochromatized Mo $K \alpha$ radiation. Intensities for two octants were collected with the $\omega$-scan technique and a scan rate of $2.5^{\circ} \mathrm{min}^{-1}$. Systematically absent reflexions and those not fulfilling the criterion $I>3 \sigma(I)$ were discarded, leaving 2411 reflexions. The data were corrected for Lorentz, polarization and absorption effects. The crystal volume was $0.0102 \mathrm{~mm}^{3}$ and transmission factors varied from $0 \cdot 199$ to $0 \cdot 348$.
The parameters of Lundgren (1953) were used as a starting model. Scattering factors of the form $f_{o}+f^{\prime}$ $+i f^{\prime \prime}$ for Ce and S and $f_{o}+f^{\prime}$ for O (Cromer \& Waber, 1965) were used. The initial refinement was performed with a block-diagonal program designed at this Institute: positional parameters and isotropic temperature factors were refined. Moreover, a separate scale factor was used for each layer to allow for systematic errors in $F_{o}$ as a function of the equi-inclination angle. $R$ fell to 0.035 for the 2411 observed reflexions. In the final refinement, anisotropic tem-
perature factors and an extinction coefficient were refined with the Brookhaven full-matrix least-squares program LINUS. Weights were calculated according to $w=\left(38+\left|F_{o}\right|+0 \cdot 007\left|F_{o}\right|^{2}+0 \cdot 00054\left|F_{o}\right|^{3}\right)^{-1}$. The final $R$ was 0.030 . A concluding difference map showed no significant peaks above the general background of $\sim 1.0 \mathrm{e}^{\AA}{ }^{-3}$. Atomic parameters are given in Table 1.*

Discussion. The previous investigation (Lundgren, 1953) was based on relatively sparse film data. The coordinates for all atoms except the $\mathrm{O}^{2-}$ ion were obtained from electron density projections. The positional parameters for $\mathrm{O}^{2-}$ were derived through geometrical considerations. No least-squares adjustment of the parameters was made. The aim of the present investigation was to obtain a more accurate determination of the coordination around Ce .

The structure is built up by infinite strings of empirical composition $\left(\mathrm{CeO}^{2+}\right)_{n}$ parallel to $\mathbf{c}$, crosslinked by $\mathrm{SO}_{4}$ groups. Fig. 1 is a projection down a showing the strings. Ce is in contact with three $\mathrm{O}^{2-}$ ions $[\mathrm{O}(6)]$ at $2 \cdot 188$ (3), $2 \cdot 269$ (3) and $2 \cdot 281$ (3) $\AA$. The $\mathrm{Ce}-\mathrm{Ce}$ distance is very short, $3 \cdot 570$ (1) $\AA$, even shorter than the $3 \cdot 63 \AA$ found in Ce metal (Lawson \& Tang, 1949). The string has also a very short $\mathrm{O}(6)-\mathrm{O}(6)$ distance, $2 \cdot 680$ (4), previously reported as $3.04 \AA$. Other distances show good agreement with the earlier work.

The $\mathrm{SO}_{4}$ group has all four O atoms bonded to Ce . It forms an almost regular tetrahedron, with mean S-O

* A list of structure factors has been deposited with the British Library Lending Division as Supplementary Publication No. SUP 31956 ( 7 pp .). Copies may be obtained through The Executive Secretary, International Union of Crystallography, 13 White Friars, Chester CH11NZ, England.

Table 1. Positional and thermal parameters
The parameters have been multiplied by $10^{5}$ for Ce and S and by $10^{4}$ for O . The temperature factor is of the form:

|  | $x$ | $y$ | $z$ | $U_{11}$ | $U_{22}$ | $U_{33}$ | $U_{12}$ | $U_{13}$ | $U_{23}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Ce | 17885 (2) | 13712 (2) | 17002 (4) | 632 (6) | 710 (7) | 647 (5) | 90 (10) | -105 (10) | -91 (10) |
| S | 47011 (8) | 20358 (11) | 34427 (23) | 662 (30) | 835 (33) | 702 (26) | -351 (46) | -210 (49) | 145 (50) |
| O(1) | 4570 (3) | 483 (4) | 5117 (9) | 111 (11) | 103 (12) | 126 (19) | -47 (18) | -48 (19) | 62 (18) |
| O(2) | 3652 (3) | 2454 (5) | 1830 (10) | 67 (10) | 188 (14) | 141 (10) | 4 (19) | -68 (18) | 102 (19) |
| $\mathrm{O}(3)$ | 623 (3) | 3152 (5) | 8772 (8) | 107 (12) | 165 (14) | 97 (12) | 39 (19) | -94 (17) | 0 (16) |
| O(4) | -16 (3) | 1677 (4) | 4358 (8) | 111 (10) | 129 (14) | 116 (11) | 18 (20) | $12(16)$ | -25 (16) |
| O(5) | 1885 (3) | 4421 (4) | 2991 (10) | 123 (13) | 160 (16) | 187 (14) | 17 (21) | -32 (21) | -64 (20) |
| O(6) | 2267 (2) | 892 (4) | 6685 (8) | 93 (10) | 86 (11) | 90 (8) | -23 (16) | 29 (16) | -15 (19) |



Fig. 1. The $\left(\mathrm{CeO}^{2+}\right)_{n}$ chains.
and O-O distances 1.476 and $2.409 \AA$ respectively (uncorrected for thermal motion).

A water molecule at $2 \cdot 587$ (4) $\AA$ completes the eightfold coordination of Ce . The coordination figure is a distorted Archimedean antiprism. The mean $\mathrm{Ce}-\mathrm{O}$ distance is $2 \cdot 366 \AA$, longer than in $\mathrm{CeO}_{2}: 2 \cdot 343$ (Magnéli \& Kihlborg, 1951), in $\mathrm{Ce}_{2}(\mathrm{OH})_{2}\left(\mathrm{SO}_{4}\right)_{3}\left(\mathrm{H}_{2} \mathrm{O}\right)_{4}: 2 \cdot 328$ (Lindgren, 1976) and in $\mathrm{Ce}\left(\mathrm{SO}_{4}\right) .4 \mathrm{H}_{2} \mathrm{O}: 2.326 \AA$ (Lindgren, 1976). The water molecules are arranged in zigzag strings also running in the $\mathbf{c}$ direction.

A stereoscopic packing diagram (Johnson, 1965) is shown in Fig. 2. Distances and angles for the present and previous investigations are given in Table 2.

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Table 2. Interatomic distances ( $\AA$ ) and angles ( ${ }^{\circ}$ )
Symmetry code: (i) $\frac{1}{2}-x,-y, z-\frac{1}{2}$; (ii) $x, y, z$; (iii) $x, y, z-1$.

|  |  | This investigation | Lundgren (1953) |
| :---: | :---: | :---: | :---: |
| $\mathrm{Ce}-\mathrm{O}(1)$ |  | $2 \cdot 340$ (3) | $2 \cdot 39$ |
| $\mathrm{Ce}-\mathrm{O}(2)$ |  | $2 \cdot 408$ (3) | $2 \cdot 45$ |
| $\mathrm{Ce}-\mathrm{O}(3)$ |  | 2.394 (4) | $2 \cdot 38$ |
| $\mathrm{Ce}-\mathrm{O}(4)$ |  | 2.463 (4) | $2 \cdot 41$ |
| $\mathrm{Ce}-\mathrm{O}(5)$ |  | 2.587 (4) | $2 \cdot 66$ |
| $\mathrm{Ce}-\mathrm{O}\left(6^{\text {i }}\right.$ ) |  | 2.188 (3) | $2 \cdot 34$ |
| $\mathrm{Ce}-\mathrm{O}\left(6^{(1)}\right)$ |  | 2.269 (3) | $2 \cdot 34$ |
| $\mathrm{Ce}-\mathrm{O}\left(6^{\text {iii }}\right.$ ) |  | 2.281 (3) | $2 \cdot 34$ |
| $\mathrm{S}-\mathrm{O}(1)$ |  | 1.484 (4) | $1 \cdot 42$ |
| $\mathrm{S}-\mathrm{O}(2)$ |  | 1.479 (4) | $1 \cdot 47$ |
| $\mathrm{S}-\mathrm{O}(3)$ |  | 1.471 (4) | $1 \cdot 46$ |
| $\mathrm{S}-\mathrm{O}$ (4) |  | 1.468 (4) | $1 \cdot 53$ |
| $\mathrm{O}(1)-\mathrm{O}(2)$ |  | 2.428 (5) | $2 \cdot 40$ |
| $\mathrm{O}(1)-\mathrm{O}(3)$ |  | $2 \cdot 388$ (5) | $2 \cdot 37$ |
| $\mathrm{O}(1)-\mathrm{O}(4)$ |  | $2 \cdot 412$ (5) | $2 \cdot 38$ |
| $\mathrm{O}(2)-\mathrm{O}(3)$ |  | 2.428 (5) | 2.36 |
| $\mathrm{O}(2)-\mathrm{O}(4)$ |  | 2.407 (5) | 2.45 |
| $\mathrm{O}(3)-\mathrm{O}(4)$ |  | $2 \cdot 393$ (5) | $2 \cdot 42$ |
| $\mathrm{O}(5)-\mathrm{O}(2)$ |  | 2.719 (5) | $2 \cdot 78$ |
| $\mathrm{O}(5)-\mathrm{O}(3)$ |  | 2.594 (5) | $2 \cdot 63$ |
| $\mathrm{O}(5)-\mathrm{O}(5)$ | (2×) | 2.789 (5) | 2.73 |
| $\mathrm{O}(6)-\mathrm{O}(6)$ | ( $2 \times$ ) | $2 \cdot 680$ (4) | 3.04 |
| $\mathrm{Ce}-\mathrm{Ce}$ | (2×) | 3.570 (1) | $3 \cdot 58$ |
| $\mathrm{O}(1)-\mathrm{S}-\mathrm{O}(2)$ |  | $110 \cdot 1$ (2) |  |
| $\mathrm{O}(1)-\mathrm{S}-\mathrm{O}(3)$ |  | $107 \cdot 9$ (2) |  |
| $\mathrm{O}(1)-\mathrm{S}-\mathrm{O}(4)$ |  | $109 \cdot 6$ (2) |  |
| $\mathrm{O}(2)-\mathrm{S}-\mathrm{O}(3)$ |  | $110 \cdot 8$ (2) |  |
| $\mathrm{O}(2)-\mathrm{S}-\mathrm{O}(4)$ |  | 109.5 (2) |  |
| $\mathrm{O}(3)-\mathrm{S}-\mathrm{O}(4)$ |  | $109 \cdot 0$ (2) |  |

## References

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Fig. 2. Stereoscopic drawing of the unit-cell contents viewed approximately along $\mathbf{c}$.

